

Analysis 1

Problem Sheet 1

Sets; maps.

Hand in: 27 January 2009

1. Exactly one of the following statements is true:

- (A) More than ten students attend the class.
- (B) Less than ten students attend the class.
- (C) At least one student attends the class.

How many students attend the class?

2. (a) Find the power sets of

- (i) $L = \emptyset$, (ii) $M = \{0\}$, (iii) $N = \{1, 2, 3\}$.

(b) Let $N = \{1, 2, 3\}$ and consider the relation \subseteq on $\mathbb{P}N$. Is \subseteq reflexive, transitive, symmetric? Does \subseteq define a total order on $\mathbb{P}N$?

3. (a) For sets A , B and C show:

- $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$,
- $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$.

(b) For sets $A, B \subset X$ show:

- $X \setminus (A \cup B) = (X \setminus A) \cap (X \setminus B)$,
- $X \setminus (A \cap B) = (X \setminus A) \cup (X \setminus B)$.

4. Let X , Y and Z be sets and $f : X \rightarrow Y$, $g : Y \rightarrow Z$ functions.

Show:

(a) If g is injective, then

$$f \text{ is injective} \iff g \circ f \text{ injective.}$$

(b) If f is surjective, then

$$g \text{ surjective} \iff g \circ f \text{ surjective.}$$